

EUROPEAN CREDIT TRANSFER AND ACCUMULATION SYSTEM (ECTS) pl. M. Skłodowskiej-Curie 5, 60-965 Poznań

# **COURSE DESCRIPTION CARD - SYLLABUS**

| Course name                          |                    |                                      |
|--------------------------------------|--------------------|--------------------------------------|
| Mathematics                          |                    |                                      |
| Course                               |                    |                                      |
| Field of study                       |                    | Year/Semester                        |
| Pharmaceutical Engineering           |                    | 1/1                                  |
| Area of study (specialization)       |                    | Profile of study                     |
|                                      |                    | general academic                     |
| Level of study                       |                    | Course offered in                    |
| First-cycle studies                  |                    | Polish                               |
| Form of study                        |                    | Requirements                         |
| full-time                            |                    | compulsory                           |
| Number of hours                      |                    |                                      |
| Lecture                              | Laboratory classes | Other (e.g. online)                  |
| 30                                   |                    |                                      |
| Tutorials                            | Projects/seminars  |                                      |
| 30                                   |                    |                                      |
| Number of credit points              |                    |                                      |
| 5                                    |                    |                                      |
| Lecturers                            |                    |                                      |
| Responsible for the course/lecturer: |                    | Responsible for the course/lecturer: |
| Dr Alina Gleska                      |                    |                                      |
| Institute of Mathematics             |                    |                                      |
| e-mail: alina.gleska@put.poznan.pl   |                    |                                      |
| phone: 61 665 2330                   |                    |                                      |
| Prerequisites                        |                    |                                      |

Student has basic knowledge of elementary functions, algebraic operations, analytical geometry, trigonometry and mathematical analysis.

Students should be able to solve simple rational equations and inequalities, to give domains of elementary functions and to know their curves.

Students seriously treat the process of studying.

#### **Course objective**

The aim of subject is introduction to complex numbers and their some practical applications. Differential and integral calculus of one variable are presented together with their applications in mathematics and chemistry.



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## **Course-related learning outcomes**

#### Knowledge

After completing the first degree studies, the graduate has expanded and in-depth knowledge of various branches of higher mathematics and detailed knowledge on the application of mathematical methods and tools in engineering and chemical sciences - K\_W2

#### Skills

After completing the first degree studies, the graduate:

- can use knowledge of higher mathematics; can build and analyse simple mathematical models; can use mathematical tools and methods, including numerical ones, to solve engineering problems - K\_U13

- is able to plan and implement self-education independently in order to raise and update their competences -  $K\_U24$ 

#### Social competences

After completing the first degree studies, the graduate:

- is aware of the deepening and expansion of knowledge to solve newly created technical problems -  $\ensuremath{\mathsf{K_K1}}$ 

- understands and appreciates the importance of intellectual honesty in own and other people's actions; is ready to demonstrate reliability, impartiality, professionalism and an ethical attitude - K\_K1

#### Methods for verifying learning outcomes and assessment criteria

Learning outcomes presented above are verified as follows:

Lecture - written exam during session

Tutorials - two long test + short tests (10 minutes) + activity

In the case of remote classes, both the exam, tests and short tests will be carried out using the eKursy.put.poznan.pl platform (each student has slightly different input data, the instructions are the same or equivalent)

Assessment criteria:

| below 50% - 2,0 | 50%-59% - 3,0 | 60%-69% - 3,5  |  |
|-----------------|---------------|----------------|--|
| 70%-79% - 4,0   | 80%-89% - 4,5 | 90%-100% - 5,0 |  |

#### **Programme content**

Complex numbers – short history; algebraic form (modulus, conjugate numbers, arithmetics, square roots), trigonometric form (de Moivre's formula, theorem about calculating roots), exponential form. Fundamental algebra theorem.



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Definition of sequences. Monotonicity, boundedness and limits of sequences. Theorem about the uniqueness of a limit. Arithmetics of proper and improper limits. The sandwich theorem (about three sequences). Definition of Euler's constant. Many examples.

Definition of a function. Domain and range of functions. Monotonicity of functions. Odd and even functions. Periodicity. Compound functions.Inverse functions.

Review of elementary functions – polynomials, power functions, exponential functions, logarithmic functions, trigonometric ones, the inverse trigonometric functions (arcus) – formulas, graphs, properties.

Limits of the functions at a point.Arithmetics of proper limits. One-handed limits. Improper limits. Asymptotes of the graphs of functions. Continuity of functions.

Definition of the derivative at a point. Geometric interpretation. Equations for a tangent line and a normal line. Rules for differentiation (especially for compound functions).

Mean value theorems and their applicastions. Extrema of functions - global and local. Criteria for existing such extrema.

Higher order derivatives. Taylor's theorem.Expansions of e<sup>x</sup>, sinx, cosx functions into Maclaurin's series.

Concavity. Points of inflection.

Indeterminate forms. De l'Hospital's theorem.

Antiderivative of a function, indefinite integrals. Integrals of elementary functions. Integration by parts and integration by substitution. Integration of rational functions. Integration of trigonometric functions (universal substitution). Integration of some irrational functions (Euler's substitutions and methods of variation of parameters).

Definition of definite integrals. Relations between indefinite and definite integrals. Integration by parts and integration by substitution for definite integrals. Geometric interpretation of definite integrals. Applications of definite integrals (areas, volumes of solids, arches length etc).

Improper integrals.

Number series. Convergence criteria for number series.

## **Teaching methods**

Lecture - multimedial presentation + examples on the blackboard

Tutorials - solving problems; discussion about obtained results

#### **Bibliography**



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Basic

- 1. W. Żakowski, Matematyka, T.1 i T.2, WNT, Warszawa 2003.
- 2. M. Gewert, Z. Skoczylas, Analiza matematyczna 1 (Definicje, twierdzenia, wzory), GiS, Wrocław 2011.
- 3. M. Gewert, Z. Skoczylas, Analiza matematyczna 1 (Przykłady i zadania), GiS, Wrocław 2011.

4. T. Jurlewicz, Z. Skoczylas, Algebra i geometria analityczna 1, (Definicje, twierdzenia, wzory), GiS, Wrocław 2007.

5. T. Jurlewicz, Z. Skoczylas, Algebra i geometria analityczna 1, (Przykłady i zadania), GiS, Wrocław 2007.

#### Additional

- 1. W. Krysicki, L. Włodarski, Analiza matematyczna w zadaniach, T.1, T.2, PWN, Warszawa 2011.
- 2. M. Grzesiak, Liczby zespolone i algebra liniowa, Wydawnictwo PP, Poznań 1999.

#### Breakdown of average student's workload

|   | Hours | ECTS |
|---|-------|------|
| Total workload  | 130   | 5,0  |
| Classes requiring direct contact with the teacher   | 70    | 2,7  |
| Student's own work (literature studies, preparation for tutorials, preparation for tests and the final exam) <sup>1</sup> | 60    | 2,3  |

<sup>&</sup>lt;sup>1</sup> delete or add other activities as appropriate